



ADVANCED MARKET RISK MODELING

Beatenberg

4 September 2003 15.30-17.00 ROLAND RASKOPF FINANCIAL STABILITY INSTITUTE

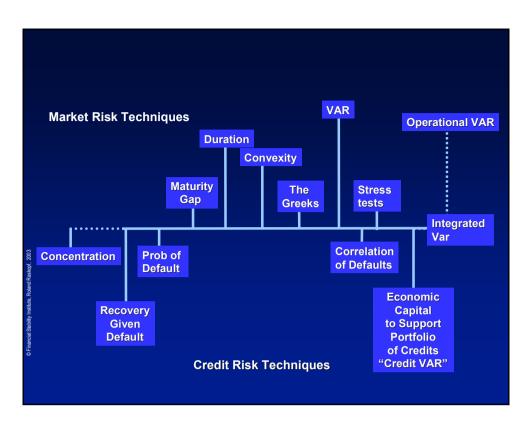
Overview

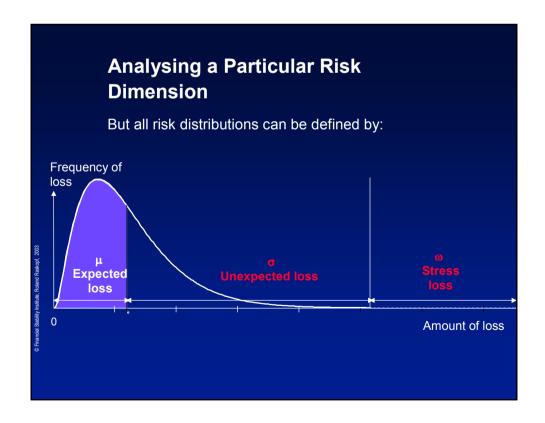
- Integrated Risk Management
- VAR Market Risk Models:
 - Variance Covariance Approach
 - Historical Simulation
 - Monte Carlo Simulation
- Backtesting
- Stress tests
- Regulatory Requirements
- Conclusion

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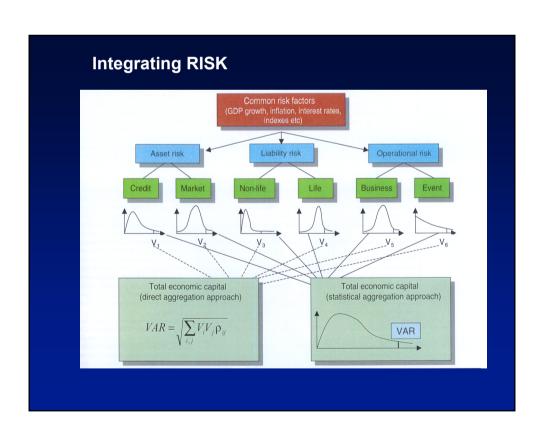






Analysing a Particular Risk Dimension Market & Credit Risk Compared

- Expected Loss (Mean of distribution)
 Charged to Revenue at Time of Transaction
- Unexpected Loss (Standard Deviation of distribution) Covered by Capital Allocation
- Stress Loss (Tail of distribution)
 Prevented by Limits or Reinsured by Underwriters





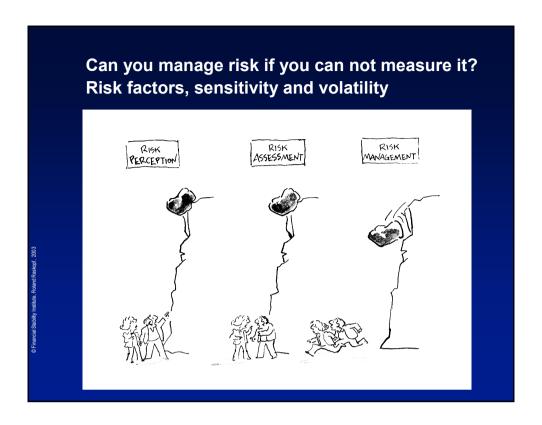
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What purpose does value at risk serve?

- Measurement of the portfolio losses which an institution will ascribe to "unfavourable circumstances"
- Standardisation of different risks for the purpose of comparability
- Quantification of limits
- Optimum allocation of resources
- Highly aggregated measure of the risks incurred for the information of management and banking supervisors

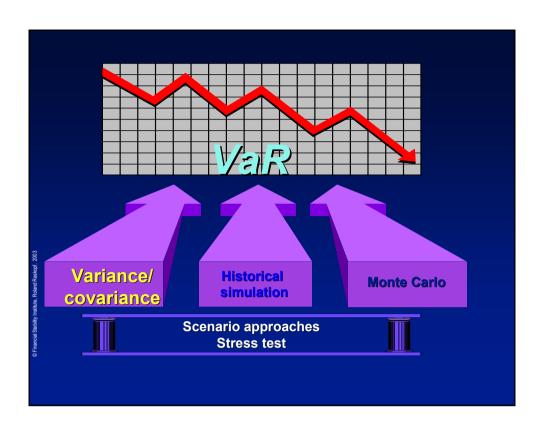
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Volatility and value at risk

- Volatilities change over time but often occur in clusters
- As volatility rises, VaR also rises

 Risk can be measured reliably only when volatilities and correlations are determined reliably

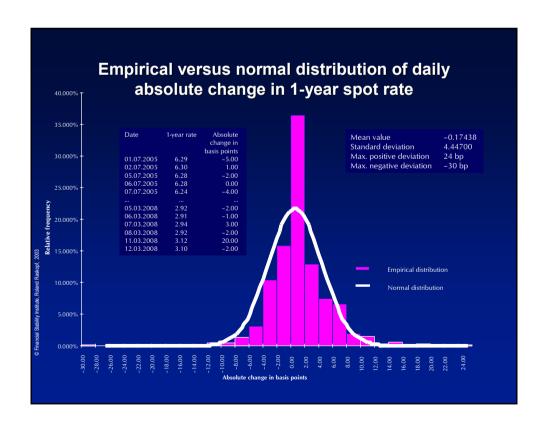
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Variance/covariance approach

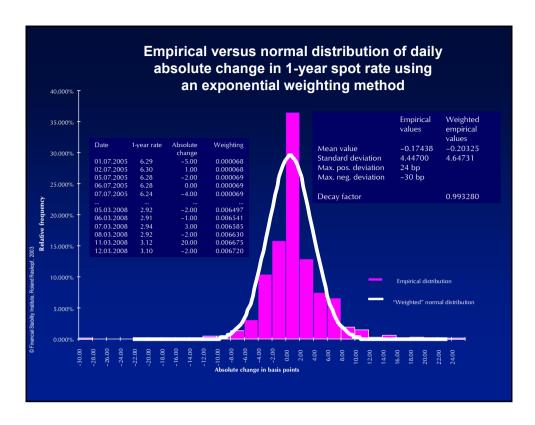
- Calculation of a portfolio's change in value as a function of:
 - the assumed extent of the risk factor changes (volatilities) and risk factor dependencies (correlations)
 - the sensitivity of the individual risk factor items (interest rates, exchange rates, shares, volatilities)
 (bank-portfolio-dependent)

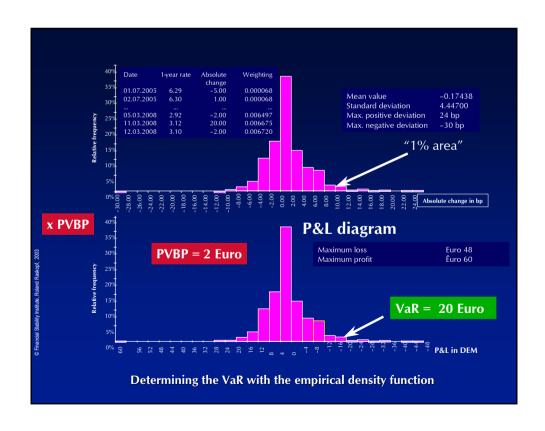




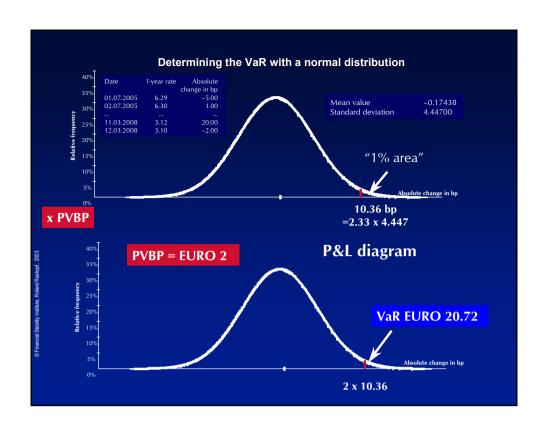


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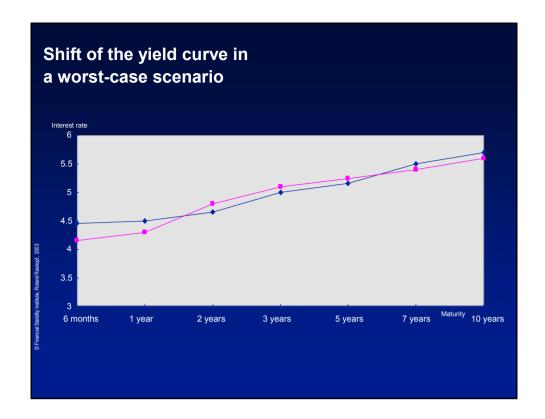


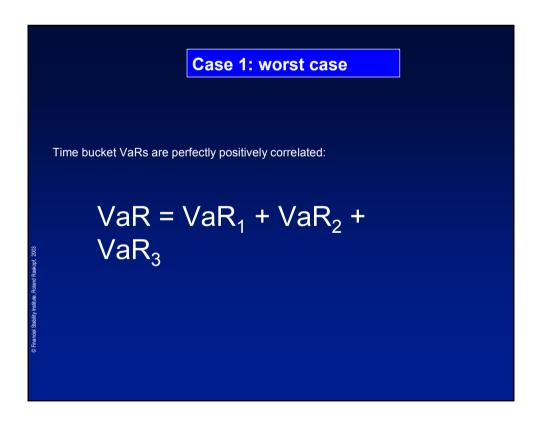




a worst-case scenario								
Total VaR in the least favourable yield scenario:								
\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	4.5.0	0 40 4	00.00	. –				
VaR = 150+80	+45+2	0+10+1	00+20) = Eu	iro 608	Ō		
Maturity	6 m	1 y	2 y	3 y	5 y	7 y	10 y	
PVBP	5	4	-3	-2	–1	10	20	
PVBP Short/long position	5 short	4 short	–3 long	–2 long	–1 long	10 short	20 short	
				_				
Short/long position	short	short	long	long	long	short	short	

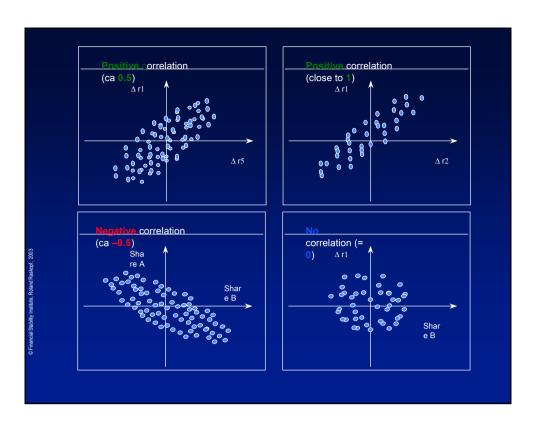


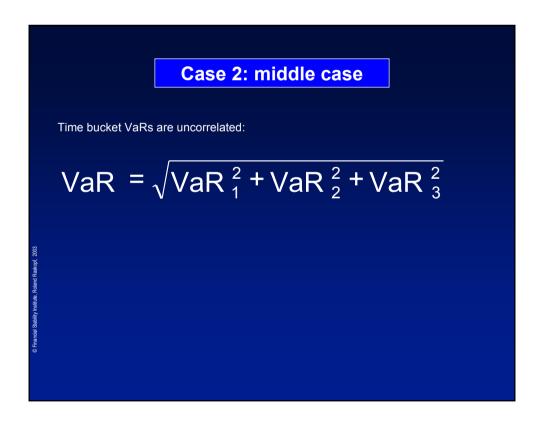




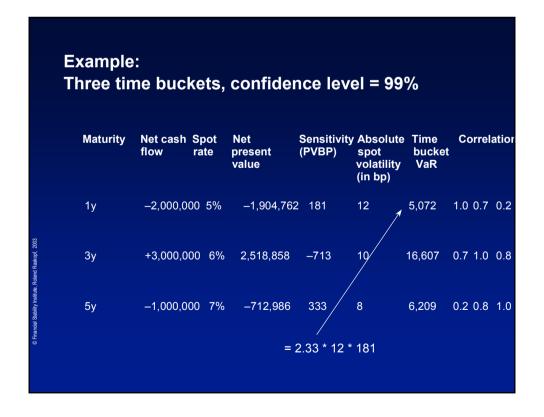


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Time bucket VaRs are correlated: $VaR_{1}^{2} + VaR_{2}^{2} + VaR_{3}^{2} + 2\rho_{1,2}(2.33\sigma_{1}PVBP_{1})(2.33\sigma_{2}PVBP_{2}) + 2\rho_{1,3}(2.33\sigma_{1}PVBP_{1})(2.33\sigma_{3}PVBP_{3}) + 2\rho_{2,3}(2.33\sigma_{2}PVBP_{2})(2.33\sigma_{3}PVBP_{3})$



Example:

Three time buckets, confidence level = 99%

Case 1: worst case

5,072 + 16,607 + 6,209 = 27,888

Case 2: middle case

 $\sqrt{5,072}$ 2 + 16,607 2 + 6,209 2 = 18,441

Case 3: normal case

5,072 2+16,607 2+6,209 2+ 2 * 0.7 * (5,072)(-16,607) + 2 * 0.2 * (5,072)(6, 209) + 2 * 0.8 * (-16,607)(6, 209)

STABILITY OF CORRELATIONS

- Correlations in key risk factors in developed markets are fairly stable.
- Some market risk factors can be assumed to be independent i.e. correlations are zero.
- In stress szenarios correlations tend towards 1 not towards 0.
- The estimation of volatilities and correlations requires historical data.
- Volatilities and correlations can be made variable with a GARCH approach.

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Advantages of the variance/covariance approach

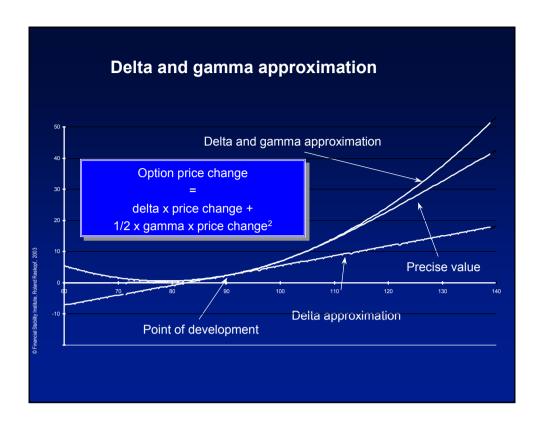
- Most common VaR approach
- Comparatively few calculations to make if:
 - second-order risks are disregarded
 - restricted to a few risk factors
- Possible to isolate individual risk factors (direct access to risk factor sensitivities: marginal value at risk)
- Input data (variances, correlation matrix) can be obtained externally (J P Morgan's RiskMetrics)

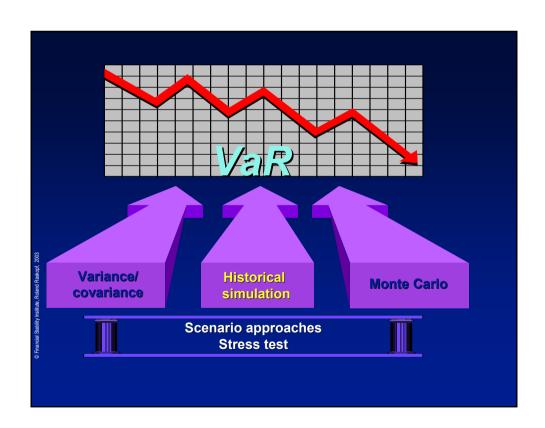
Problems/criticisms regarding variance/covariance approach

- · Second-order risks of options (convexity risks) are disregarded
- Limited to a small number of specified risk factors
- A specific distribution assumption (inter alia, normal distribution) is taken as a basis
- · Fat tails are disregarded
- Stability assumed for volatilities and correlations

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Example: historical simulation

- Determination of 10-day changes on the basis of historical risk parameters
- Arrangement of changes in ascending order and elimination of the five lowest values
- VaR = sixth-lowest value

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Example: historical simulation 10-day change -90 -70 -60 -55 -50 -45 = VaR -40 ... 99% confidence interval, i.e. the sixth value of 500 values.

Historical simulation

 Valuation of current portfolio on the basis of historical risk parameters:

PV₁, PV₂, ..., PV₅₁₀

 Determination of portfolio changes for a defined holding period (here: 10 days):

 $\Delta \Pi_{\varsigma_1} = PV_{11} - PV_1$ $\Delta \Pi_{\varsigma_2} = PV_{12} - PV_2$...

 $\Delta \Pi \varsigma_{500} = PV_{510} - PV_{500}$

Advantages of historical simulation

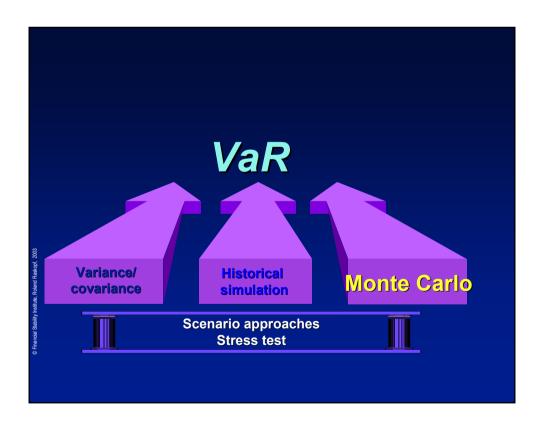
- Exact reproduction of historical reality
- Independent of any distribution assumption
- Historical correlations, variances implicitly taken into account
- Capture of second-order risks

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Problems / criticisms

- Extremely resource-intensive storage and calculation process
- Purely past-oriented
- No sensitivities recognisable



Monte Carlo simulation

- The variance/covariance approach and historical simulation are purely past-oriented
- Monte Carlo simulation offers the possibility of determining random paths for risk factors on the basis of historically calculated or impliedly determined statistical quantities
- In addition to VaR estimates, Monte Carlo methods are used for valuing complex derivatives (e.g. pathdependent options) for which there is no analytical solution

Monte Carlo simulation procedure

- Determining input data (historical or implied variances and correlations)
- · Generating random-event-dependent risk factor paths
- Determining P&L for each path status
- Eliminating 1% to remove worst cases
- VaR = worst value left over

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Generating random paths with geometrical Brownian motion

 The risk factor (e.g. periodical yield, share price, exchange rate, volatility) changes over time as follows:

$$\Delta lnS = \mu \Delta t + \epsilon \sigma \sqrt{\Delta t}$$

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Example: creating a risk factor path for the DAX

 $\begin{array}{ll} \text{Given} & \quad \mu_{\text{daily}} = 0.00046 \\ & \quad \sigma_{\text{daily}} = 0.00962 \\ & \quad \text{DAX} = 2,700 \end{array}$

$$\Delta \ln DAX = \mu_{daily} + \varepsilon \times \sigma_{daily} = 0.00046 + \varepsilon \times 0.00962$$

$$t = 0: DAX_0 = 2700$$

Carrying out a (normally distributed) random experiment: ϵ = 0.52

 $t = 1: \Delta \ln DAX = \ln DAX_1 - \ln DAX_0 = 0.00046 + 0.52 \times 0.00962 = 0.0055$ $\Rightarrow \ln DAX_1 = \ln DAX_0 + 0.0055$ $\Rightarrow DAX_1 = DAX_0 \times e^{0.0055} = 2,715$

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Creating a risk factor path

Carrying out a (normally distributed) random experiment: ε = -0.11

$$t = 2$$
: $\Delta \ln DAX = \ln DAX_2 - \ln DAX_1 = 0.00046 - 0.11 \times 0.00962 = -0.0006$
 $\Rightarrow \ln DAX_2 = \ln DAX_1 - 0.0006$
 $\Rightarrow DAX_2 = DAX_1 \times e^{-0.0006} = 2,713$

Thus a two-step Monte Carlo path is created for the DAX, with:

$$DAX_1 = 2,715$$

 $DAX_2 = 2,713$

Monte Carlo Simulation

Basic ideas:

- Produce numerous changes in portfolio value with the help of a random generator
- assumption: the probability distribution of risk factors is known
- common approach: the daily logarithmic risk factor changes are multivariate normally distributed

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Monte Carlo simulation

 distribution assumption: multivariate normal distribution:

$$\left(X_{t+1}^1, \ldots, X_{t+1}^n\right) \sim N\!\!\left(\boldsymbol{\mu}, \!\boldsymbol{\Sigma}\right)$$

$$\mu = (\mu_1, ..., \mu_n)$$

$$\Sigma = \begin{pmatrix} \sigma_1^2 & \cdots & \rho_{1,n} \sigma_1 \sigma_n \\ \vdots & \ddots & \vdots \\ \rho_{1,n} \sigma_1 \sigma_n & \cdots & \sigma_n^2 \end{pmatrix}$$

Monte Carlo simulation

• Problem:

the parameters μ and Σ are unknown:

- \Rightarrow estimation of the parameters μ_i , σ_i and $\rho_{i,j}$ from historical data
- additional assumption:

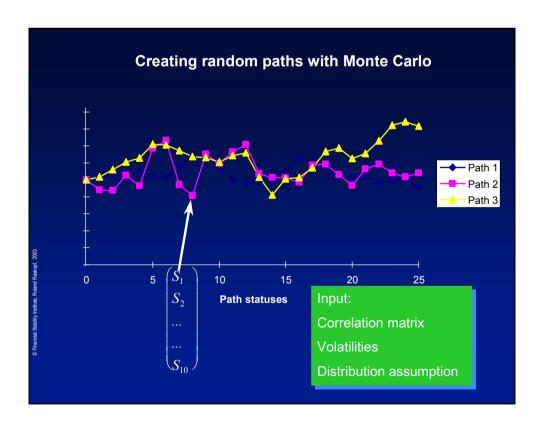
$$\mu_i$$
 = 0 for i = 1,...,n

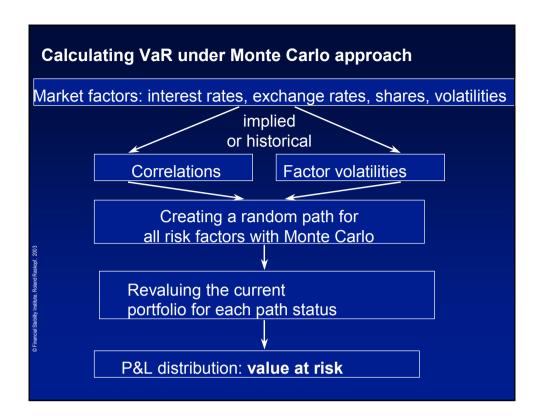
 After estimation of the parameters the normal distribution is completely known

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Monte Carlo simulation $Cholesky \ decomposition:$ $C = AA^T$ $A = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1i} \\ a_{21} & a_{22} & \cdots & a_{2i} \\ \vdots & \vdots & \ddots & \vdots \\ a_{j1} & a_{j2} & \cdots & a_{ji} \end{bmatrix}$ $a_{ji} = \begin{cases} 0 & \text{for } j < i \\ \sqrt{c_{ji} - \sum_{k=1}^{i-1} a_{jk}^2} & \text{for } j = i \\ \frac{1}{a_{ji}} \sqrt{c_{ji} - \sum_{k=1}^{i-1} a_{jk} a_{jk}} & \text{for } j > i \end{cases}$ $c_{ij} = \text{cov}(i, j)$





Advantages

- Although the input data are usually past-oriented, random-event-dependent risk factor paths can be generated
- Very flexible to handle. Different distribution assumptions can be made for different risk factors (e.g. fat tails are taken into account, leptokurtosis is possible)

Capture of second-order risks

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Problems/criticisms

- Extensive calculation involved; entire portfolio has to be revalued for each path status
- No stable solution with short Monte Carlo path
- Distribution assumption of disturbance term

• Usefulness of random generator questionable

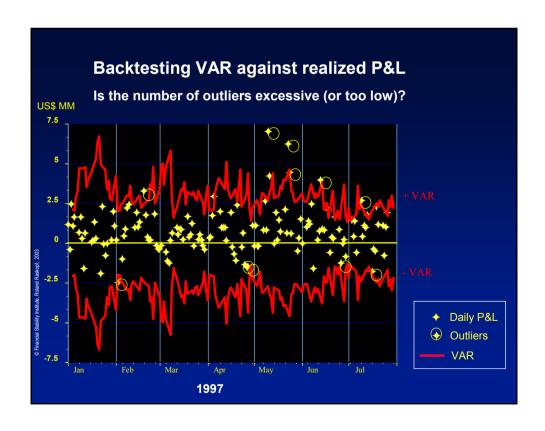
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Summary: Comparison of VAR approaches

	Variance- Covariance	Historical sin	Historical simulation Partial Full	
Position valuation	Delta	Delta- gamma-vega	Full revaluation	Full revaluation
Distribution assumption	Normal	Non-normal (historical)	Non-normal (historical)	Non-normal (implied)
Cost	Low	Medium	High	High
Drawbacks	Reliance on history; linearity	Reliance on history; extreme events	Reliance on history	Reliance on historical correlations

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Establishing the increase factor

Zone	Number of outliers	Increase factor	Cumulative probability	
	0	0.00	8.11%	
	1	0.00	28.58%	
Green	2	0.00	54.32%	
	3	0.00	75.81%	
	4	0.00	89.22%	
	5	0.40	95.88%	
	6	0.50	98.63%	
Yellow	7	0.65	99.60%	
	8	0.75	99.89%	
	9	0.85	99.97%	
Red	10 or more	1.00	99.99%	

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Stress tests

Standard risk measures (e.g. VaR) do not take into account stress events sufficiently, therefore...

- A routine and rigorous programme of stress testing should be in place
- Results should be reviewed periodically by senior management
- If vulnerabilities are revealed prompt steps must be taken to manage those risks appropriately
- ⇒ "Stress testing" as generic term describing various techniques used by financial firms to gauge their potential vulnerability to exceptional, but plausible, events
- ⇒ See CGFS publications from April 2001 and April 2000

Stress testing - some conclusions beforehand

- Sound risk management makes extensive use of stress tests
- If you have to make the choice: rather rely on expert judgement than on the model

"The discipline of concentration in the essential elements is the secret of success." Reinhold Messner

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Positive aspects...

- Stress tests are easy to understand for management (no assumptions like at VaR, ...)
- Stress tests supplement Value at Risk (VaR) as VaR is of limited use in measuring firms' exposures to extreme market events
- Stress Testing calls on the judgement of risk managers and senior executives to assess whether, and to what degree, the firm should handle an exposure ...

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but also challenges ...

- What is a stress scenario, i.e. how much should risk factors be changed for a stress scenario to be given?
- Crashes in market prices are rare events. Can one estimate a crash in future relying on crashes experienced in the past?
- For a stress scenario to be defined, the portfolio itself needs a thorough analysis beforehand: Where are the loop holes? What are the most important risk factors?
- As portfolios change, there is a need for **updating**
- Valuation with approximation is not fully satisfactory, even a full revaluation on grid points can be problematic

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and limitations...

- A Stress test estimates the exposure to a specified event, but <u>not the probability</u> of such an event occurring.
- Numerous decisions in the specification of a stress test must be made that rely on the judgement and experience of the risk manager.
- No guarantee that the risk manager will chose the "right" scenarios or interpret the results effectively.
- Stress tests impose significant computational cost (collecting data from diverse business units, need to revalue complex options-based positions).
- At present firms cannot integrate market and credit risks in a systematic way in their stress tests.

How to derive stress tests

- Historic scenarios (crash, crisis)
 - equity crash 1987
 - emerging market crisis (SE Asia) 1997
 - russian debt problems 1998
- Historic market movements
- Makro-research
 - expert-scenorios
- Correlation breakdown, correlation setting
- Portfolio scenarios

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	Stress testing	j techniques
	Technique	Stress test result:
	Simple sensitivity test	Change in portfolio value for one or more shocks to a single risk factor
2003	Scenario analysis	Change in portfolio value if the scenario were to occur
arcial Sability Institute. Roland Raskopti. 2	Maximum loss	Sum of individual trading units' worst case scenarios
© Financial Sability	Extreme value	Probability distribution of extreme losses

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Supervisory Quantitative Requirements

The Quantitative Part of the Model:

- 10 days Holding Period
- 99% Confidence Level
- Full Usage of Risk Factor Correlations
- Observation Period

But ...

Supervisory Qualitative Requirements

... the qualitative aspects on <u>how a model is implemented</u> are most important:

- Ensure that risks are measured accurately and with integrity
- The standards include the following:
 - Independent risk control unit
 - . Regular back testing
 - . Senior management must be actively involved
 - Model must be closely integrated into day-to-day risk management process
 - Independent review of overall risk management process regular part of internal audit

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Supervisory Review Process Scoring - Setting the Scaling Factor for Regulatory Capital - Organisation of Trading Activities / Organisational Environment 0.30 - Front Office, Middle Office, Back Office x - Risk Controlling x - Internal Audit x - Model Input 0.20 - Trade / Position Data (Timeliness) x - Market Data (Quality) x

Supervisory Review Process Scoring - Setting the Scaling Factor for Regula	ılatory Capital	
Model	0.20	
Instrument Models	x	
Adequacy of Risk Factors, Stripping and Mapping	x	
Adequacy of Stochastic Modeling	x	
Model Use in Risk Control	0.30	
Limit System	x	
Management Information and Reporting	x	
Stress Tests	x	

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Models useful in difficult markets?

- Limited information
- Limited access to the market
- High volatility
- Concentration of instruments/players
- Poor settlement procedures
- Regulation
- High sensitivity to political considerations & commodity cycle

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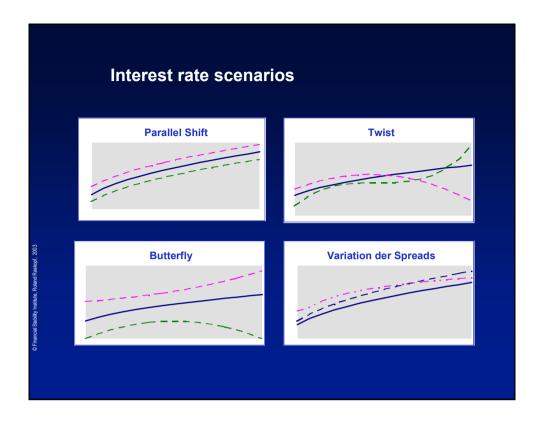
Conclusion

- MR Models are just tools but no "crystal balls"
- Capital allocation and models
- Black boxes are useless
- Main Problem: DATA
- Improved the risk culture and EDP environment
- Event risk approach
 - stress-testing
 - contingency plans
- Integrated approaches are key in difficult markets

ANNEX Stresstests

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DPG Stress Testing Standards

- Parallel yield curve shifts of 100 basis points up and down;
- Steepening and flattening of the yield curves (2s to 10s) by 25 basis points;
- Each of the 4 permutations of a parallel yield curve shift of 100 basis points concurrent with a tilting of the yield curve (2s and 10s) by 25 basis points;
- Increase and decrease in all 3-month yield volatilities by 20% of prevailing levels;
- Increase and decrease in equity index values by 10%;
- Increase and decrease in equity index volatilities by 20% of prevailing levels;
- Increase and decrease in the exchange value (relative to the US dollar) of foreign currencies by 6%, in the case of major currencies, and 20%, in the case of other currencies;
- Increase and decrease in foreign exchange rate volatilities by 20% of prevailing levels; and
- Increase and decrease in swap spreads by 20 basis points.

Source: DPG, A Framework for Voluntary Oversight, February 1995, p.30.



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Stress Sce	nario: C	reuit Spre	au			
Desk	Market Exposure (in \$mill)	1bp Spread Widening (in Sthous)	Shock Widening (basis point)	Loss Impact (in \$mill)	Impact Limit	% of Limit
Corporate Bonds						
Corporate Bond Rating						
AAA	125	88	20	(1.75)		
AA	75	53	30	(1.58)		
A	(5)	(4)	45	0.16		
BBB	25	18	70	(1.23)		
Portfolio Hedges						
Swap (Corporate Bond Index)	(15)	(11)	50	0.53		
Swap (Interest Rate)	(5)	(4)	30	0.11		
Total Corporates:				(3.76)	10	38%
Global Emerging Debt Markets						
High 2-4yrs	-10	(7)	2,400	5.50		
High 4+yrs	12	8	2,100	(6.00)		
Medium	11	8	500	(3.85)		
Low	15	11	250	(2.63)		
Total Emerging Markets:				(6.98)	10	70%
* adjusted for convexity			,			



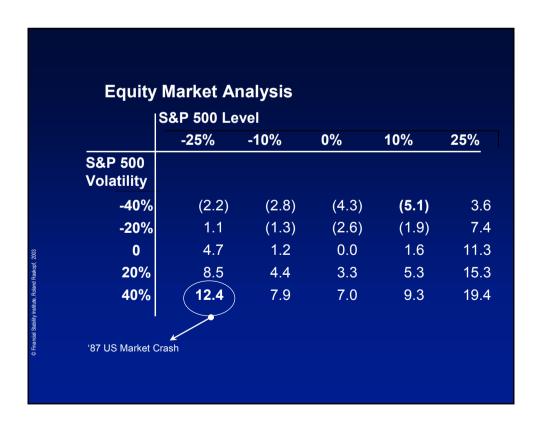
	Default Sc	enario				
		Par	Price	Mkt Val (US\$ in MM)	Recovery	IMPACT (US\$ in MM)
	Hard Currency Bonds:					
	IANs	USD10MM	60%	6.0	10%	<5.4>
	PRINs	USD 6MM	60%	3.6	10%	<3.2>
	MinFin3s	USD 5MM	70%	3.5	15%	<3.0>
	Russia 10.0% Jun'07s	USD15MM	70%	10.5	15%	<8.9>
	Local Mkts: Bonds & Bills					
	GKOs/OFZs (RUR/\$ = 6)	RUR90MM	50%	7.5	10%	<6.8>
5003	Local Mistor Foreign Evolun					
copf,	Local Mkts: Foreign Exchan FX Deposits with Russian bar		6.0	2.0	0.0	<2.0>
d Ras	FX Deposits with Western bar		6.0	4.0	12.0*	<2.0>
, Rolan	1 A Deposits with Western bar	IKS INDINZAMIM	0.0	4.0	12.0	\2.0>
stitute	Equity:					
Stability In	Equity (Various)			5.0	20%	<4.0>
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Hypothetical Economic Scenario

- The Modest Recession Case: (12 month horizon)
 - the following changes will gradually occur in the first six months and the conditions will remain unchanged for the remaining six months
 - > Inflation expectations rise one percent
 - ➤ Bond yields rise 150 basis points
 - > Equity market valuations decline 20%
 - Credit spreads widen approximately one-third the move observed in Fall 98
- The Severe Recession Case: (18 month horizon)
 - the following changes will gradually occur in the first twelve months and the conditions will remain unchanged for the remaining six months
 - > Inflation expectations rise two percent
 - ➤ Bond yields rise 300 basis points
 - > Equity market valuations decline 35%
 - Credit spreads widen approximately two-thirds the move observed in Fall 98

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